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Approach to accurately measuring the speed of optical precursors

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Precursors can serve as a bound on the speed of information with dispersive medium. We propose a method to identify the speed of optical wavefronts using polarization-based interference in a solid-state device, which can bound the accuracy of the speed of wavefronts to less than 10^{-4} with conventional experimental conditions. Our proposal may have important implications for optical communications and fast information processing.

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The advent of fast information processing in quantum network devices often raises the need for accurate control of light pulse propagation. The speed of the information encoded on the optical pulse should obey the causality [1]. This seemingly obvious fact has been experimentally proved only recently [2]. Unlike the well-defined velocity of a point particle, the velocity of a light pulse traveling through an optical material is not precisely defined. The motion of a light pulse can be approximated by the group velocity (v_g), which is given by $v_g = c/(n + \omega dn/d\omega)$, where c is the speed of light in a vacuum, n is the refractive index of the material and ω is the frequency of the light [3]. It can be clearly seen that v_g can be greater than c and even be negative when $\omega dn/d\omega$ is negative (anomalous dispersion). Experimental studies of fast light propagation include Refs. [2, 4–7]. To resolve the apparent contradictions between fast light propagation and the theory of relativity, optical precursors were introduced by Sommerfeld and Brillouin in 1914 [8–10]. The theory states that the front edges of an ideal step-modulated pulse propagate at speed c because of the finite response time of any physical material and no components can overtake this wave front. The forerunners, now known as Sommerfeld-Brillouin precursors, are followed by the main pulse traveling at its group velocity. This conclusion, while conceptually clear, lacks of experimental evidence directly relating to the speed of optical precursors.

Optical precursors are recently of great interest because they have applications in biomedical imaging [11], underwater communications [12], and the generation of high peak power optical pulses [13, 14]. A number of theoretical and experimental studies have been carried out [15–21]. Specifically, direct observation of precursors which are separated from the delayed main fields has been achieved with electromagnetically induced transparency (EIT) in cold atoms [20, 21]. For all these works, the authors claim that the rising edge of the input pulse propagates at the speed of c in the form of Sommerfeld precursors. However, considering the rise time of the detecting systems, a time delay of shorter than 1 ps would not be captured if the precursors travel at a speed which differs little from c.

In this paper, we propose an experimental method to precisely determine the speed of optical wavefronts propagating through a dispersive medium, i.e., optically pumped Nd^{3+}:YVO_4 crystal by interference with a reference pulse traveling through a pure YVO_4 crystal. If there is any speed difference between wavefronts in the Nd^{3+}:YVO_4 crystal and the YVO_4 crystal, the interference pattern will be significantly altered and reveal the influence of Nd^{3+} ions on the speed of the wavefronts.

Nd^{3+}:YVO_4 crystals (doping level, 10 ppm.) have been systematically investigated as a candidate solid-state quantum memory [22–24]. The $^4I_{9/2} \rightarrow \,^4F_{3/2}$ transition of Nd^{3+} around 879.705 nm has a narrow homogenous linewidth (Γ_h ~63 kHz) and wideband inhomogeneous broadening (Γ_{inh} ~2.1 GHz) at low temperature. Nd^{3+} is a Kramers ion and thus has strong first-order Zeeman effect, which yields a large ground-state splitting under the application of a magnetic field (10-100 GHz/T). From the inset of Fig. 1, it can be seen that a moderate magnetic field splits the ground states into two Zeeman spin levels ($|1\rangle, |2\rangle$) which connect to an excited state ($|3\rangle$). Thus, this provides a Λ-like system [23, 24].

Note that any real pulse has a step-rising front which is composed of the infinite spectral components, even the pure YVO_4 crystal cannot response to it, the ideal step-rising wave front propagates at the speed of c independent of any medium. While for the light pulse produced by electro-optic modulator (EOM) with a finite rise time, the YVO_4 crystal behaves as a wideband response medium, the wave fronts which travels at the speed of c are generally too weak for detection in the YVO_4 crystal. In both the Nd^{3+}:YVO_4 crystal and the pure YVO_4 crystal the experimentally detectable wavefront should propagate at the same speed $v_0 = c/n_0$, where n_0 is the refractive index for far-detuned frequency components of the input pulse. The refractive index ideally reaches unity and v_0 becomes c for infinite frequency components. In the Nd^{3+}:YVO_4 crystal, the optically pumped Nd^{3+} ions have a strong dispersion of the narrow-band frequency components that is near the resonance line of the Nd^{3+}. Those components make up the greatly delayed or accelerated main pulse.

The frequency of the probe light is tuned to the Nd^{3+} absorption line (ω_{31}). It is a square pulse modulated using an EOM with a temporal width of $t_0 = 4 \times 10^{-6}$ s and a rise (fall) time of $t_r = 0.1 \times 10^{-9}$ s. The input light intensity is assumed to be unity in the following calculations. $E(0, \omega)$ is the Fourier transform of the input pulse. The Nd^{3+}:YVO_4 crystal under-
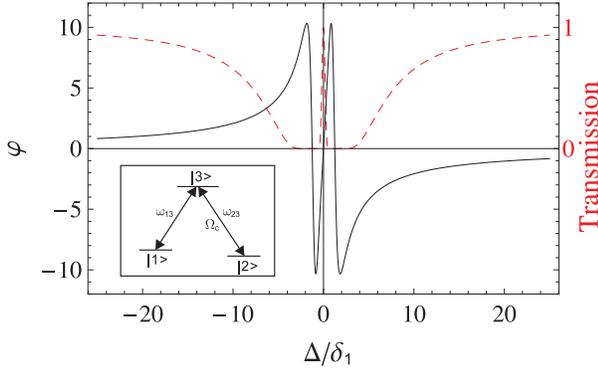
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FIG. 1: (Color online. The phase (black solid line) and intensity (red dashed line) of light after passing through a Nd^{3+}:YVO_4 crystal versus the probe detuning. The inset is an energy level diagram of the $^4I_{9/2} \rightarrow {}^4F_{3/2}$ transition of Nd^{3+} under a magnetic field.

going EIT is characterized by its linear susceptibility [25]

$$\chi_1(\omega) = \frac{\alpha_0}{k_0} \frac{4(\Delta + i\gamma_{12})\delta_1}{|\Omega_c|^2 - 4(\Delta + i\gamma_{12})(\Delta + i\delta_1)}, \quad (1)$$

where $\alpha_0 = 4130$ m^{-1} is the on-resonance absorption coefficient; $k_0 = n_0\omega_{31}/c = 1.55 \times 10^7$ m^{-1}; n_0 is the refractive index of the YVO_4 crystal near 879.705 nm for light polarized parallel to the crystal's symmetric c axis [26]; $\Delta = \omega - \omega_{31}$ is the probe detuning; and Ω_c is the coupling laser Rabi frequency. $2\delta_1$ is the original absorption bandwidth, which is controlled by the pumping procedure. Here, we choose $\delta_1 = 2\pi \times 1$ MHz which is larger than Γ_h. The dephasing rate between the two ground states is $\gamma_{12} = 2\pi \times 0.2$ kHz. These parameters were chosen based on experimental observations [23, 24]. The transmitted field is given by $E(z_1, \omega) = E(0, \omega)Exp[ik_1(\omega)z_1]$ with $k_1(\omega) = k_0\sqrt{1 + \chi_1(\omega)} \simeq k_0(1 + \chi_1(\omega)/2)$. Via a fast Fourier transformation (FFT), the transmitted field in time domain can be obtained. There have been some analytical solutions to this problem [19], which fit well with the results obtained using the FFT. However, to preserve the phase of the field for the coming interference experiments, we use FFT to evaluate the integrals. Fig. 1 shows the phase of the photons experiencing $\varphi = Re[k_1(\omega)z_1] - k_0z_1$ with $z_1 = 0.01$ m and the transmitted-field intensity of $Exp[-2Im[k_1(\omega)z_1]]$. It can be seen that far-detuned light experiences a smaller phase shift than near-resonance light. After passing through the EIT medium, the rising and falling edges at $t = 0$ and $t = t_0$ should not experience group delay caused by Nd^{3+} ions. However, the main fields are approximately delayed by $t_g = 2\alpha_0z_1\delta_1/|\Omega_c|^2$ [19, 20].

The experimental scheme is shown in Fig. 2. The laser should be wavelength tunable and have a linewidth well below 1 MHz. Using a polarization beam splitter (PBS) and a half-wave plate (HWP), the light's polarization can be tuned to maximal absorption for a Nd^{3+}:YVO_4 crystal. The top acousto-optical modulators (AOM) shift the laser frequency to be on-resonance with ω_{23} to serve as the coupling light. The middle of the AOM sweep of the laser frequency around
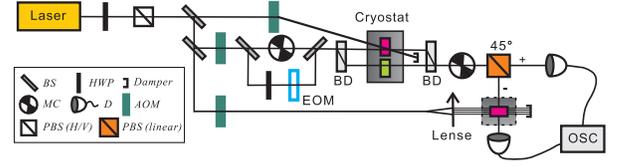

FIG. 2: (Color online) Experimental setup for measuring the speed of optical wavefronts. The coupling light produced by the top AOM should overlap with the probe light in the first Nd^{3+}:YVO_4 crystal (top, red filled) and be damped then. The pump light for the the first Nd^{3+}:YVO_4 crystal is produced by the middle of the AOM and it is controlled by a MC. The input pulse is produced by the EOM. The lower AOM produces the pump light for the filter. The pure YVO_4 crystal (bottom, green filled) is used as a reference path. After passing through the BD, the light undergoes polarization-dependent detection which is recorded on an oscilloscope (OSC).

ω_{13} serves as the pump light. The mechanical chopper (MC) before the BD turns the strong pump light off during the detection cycle. The input pulse is generated using a 15-GHz EOM and the light's polarization is rotated to $|+\rangle = \frac{1}{\sqrt{2}}(|H\rangle + |V\rangle)$ by the HWP, where H and V denote horizontal and vertical polarization state, respectively. To show that the wavefronts actually do travel at the speed of v_0 independently of the Nd^{3+} ions, we use a reference pulse traveling through a pure YVO_4 crystal. The beam displacer (BD) separates H and V polarized light. The H polarized probe light is sent through the Nd^{3+}:YVO_4 crystal (top, red filled) such that it overlaps with coupling light at a small angle. The V polarized probe light is sent through the pure YVO_4 crystal (bottom, green filled) of the same length, z_1. The Nd^{3+}:YVO_4 crystal's c axis is aligned in the horizontal direction and the YVO_4 crystal's c axis is aligned in the vertical direction to avoid birefringence. All of the crystals are placed in a cryostat with a temperature 3 K and a magnetic field 0.5 T. Then H and V polarized light are combined using the BD and then undergo polarization dependent detection. The MC after the BD is used to block light to protect the filter and detectors during the pumping procedure of the first Nd^{3+}:YVO_4 crystal. The transmitted light intensities for the $|+\rangle$ and $|-\rangle = \frac{1}{\sqrt{2}}(|H\rangle - |V\rangle)$ polarizations are recorded using an oscilloscope (OSC). The intensities are given by

$$I_+(z_1, t) = |IFT\{\frac{1}{\sqrt{2}}[E_H(z_1, \omega) + E_V(z_1, \omega)]\}|^2 \quad (2)$$

$$I_-(z_1, t) = |IFT\{\frac{1}{\sqrt{2}}[E_H(z_1, \omega) - E_V(z_1, \omega)]\}|^2, \quad (3)$$

where

$$E_H(z_1, \omega) = \sqrt{1/2}E(0, \omega)Exp[ik_1(\omega)z_1], \quad (4)$$

$$E_V(z_1, \omega) = \sqrt{1/2}E(0, \omega)Exp[ik_0z_1] \quad (5)$$

and IFT means Inverse Fourier Transformation. Note that the phase velocity is the relevant quantity for interference, which is the same in a pure crystal and a low-doping crystal. If the H polarized field and V polarized field arrive at the same time,

the interference shall give an ideal near-to-zero output for I_- in the first nanoseconds.

To totally eliminate the main fields with the central frequency components, which experience greater phase shifts, another Nd^{3+}:YVO_4 crystal with length z_2 is placed before the detectors for $|-\rangle$ polarized light. The crystal's c axis is aligned in the $-45°$ direction for maximal absorption. It acts as a strong absorption filter which can be characterized by

$$\chi_2(\omega) = \frac{\alpha_0}{k_0} \frac{\delta_2}{-(\Delta + i\delta_2)}. \qquad (6)$$

This is the special case of Eq. (1) with $\Omega_c = 0$. δ_2 is controlled by the pump light produced by the lower AOM in Fig. 2. In the following text, we refer to this Nd^{3+}:YVO_4 crystal as the "filter" for simplicity. With the filter present, the recorded intensity for I_- is given by

$$I_-(z_2, t) = |IFT\{\frac{1}{\sqrt{2}}[E_H(z_1, \omega) - E_V(z_1, \omega)]e^{ik_2(\omega)z_2}\}|^2, \quad (7)$$

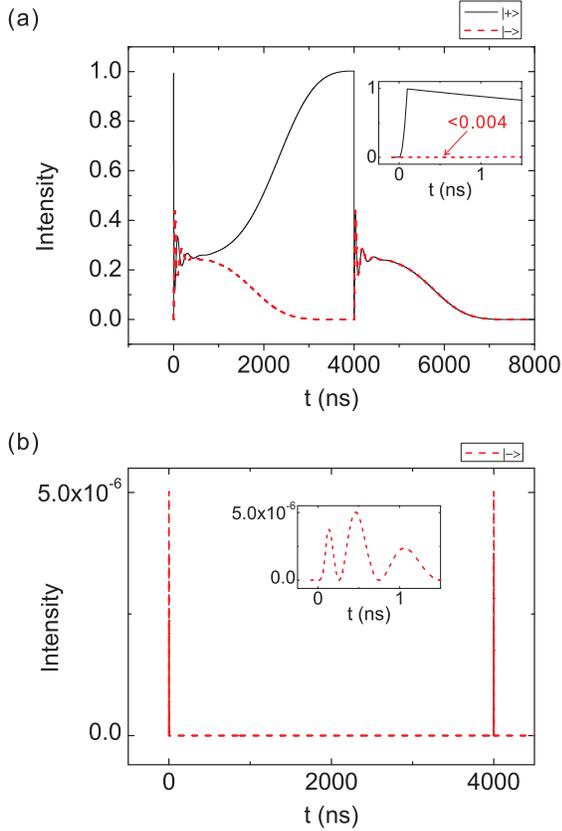where $k_2(\omega) \simeq k_0(1 + \chi_2(\omega)/2)$.

(a)

(b)

FIG. 3: (color online). Intensity of the transmitted light of the polarizations $|+\rangle$ (black solid line) and $|-\rangle$ (red dashed line) without the filter (a) and with the filter (b).

To show the advantages of having the filter present, the simulation results using FFT with 0.01-ns sampling resolution are shown in Fig. 3 with $z_1 = 0.01$ m and $z_2 = 0$ for panel (a) and

$z_1 = 0.01$ m and $z_2 = 0.01$ m for panel (b). The input pulse is the same as before and δ_2 was chosen to be $150\delta_1$. For Fig. 3(a), we first note that the V polarized light remains the same as the input square pulse after traveling in the pure YVO_4 crystal as mentioned above. When the H polarized wavefronts decay, the V polarized light starts to dominate. Therefore, I_+ (black solid line) and I_- (red dashed line) have nearly the same intensity. Then, the H polarized main fields slowly increase. I_+ rises with it and I_- decays, because the delayed main fields are still almost entirely in the phase with the V polarized light. After $4\ \mu s$, the V polarized pulse ends, and I_+ and I_- share exactly the same intensities. It can be seen that I_+ rises immediately after $t = 0$, but I_- is suppressed during the first nanosecond. This shows that H polarized wavefronts travel at the same speed as the V polarized light in the pure YVO_4 crystal. If this were not the case, I_- would rise at the same time and with the same intensity as I_+, because only H (V) polarized light would present and there would be no interference between the two paths for the given delay time. A time delay τ_d between the arrival of H and V polarized light would lead to a remarkable intensity for I_-, which can be estimated to be τ_d/t_r. However, for Fig. 3(a) with no filter present, I_- can grow to 0.004 in the first nanoseconds with no delay for either path. Therefore, it becomes impossible to measure τ_d with subpicosecond accuracy.

The transmission $I_-(z_2, t)$ with the filter is shown in Fig. 3(b). I_+ is the same as that in Fig. 3(a) and is not shown in Fig. 3(b). Because the filter has wideband absorption, only photons with frequencies far-detuned from the resonance are transmitted. The main fields are totally absorbed by the filter, and only rising and falling edges at $t = 0$ and $t = t_0$ remain. For all time scales, at most I_- can grow to 5×10^{-6} in the first nanoseconds after $t = 0$ and $t = t_0$. Because the remaining far-detuned light experiences little phase shift, there is near-perfect interference between the two paths. Therefore, whenever there is an intensity larger than 10^{-5} recorded for I_-, we may infer that there is a time delay between the arrival of H and V polarized light. Moreover, the interference yields the same results when the first Nd^{3+}:YVO_4 crystal acts as a two-level system, which is the fast-light regime.
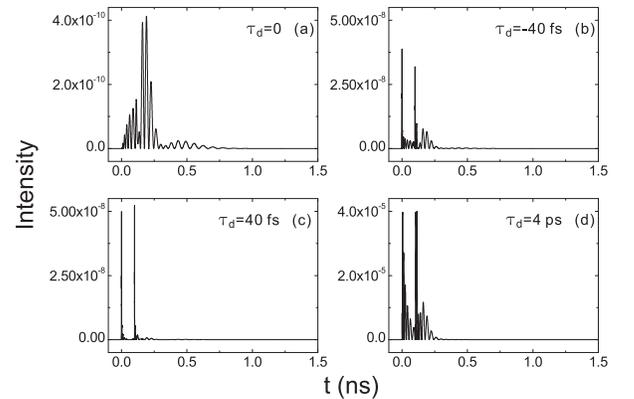

FIG. 4: Intensity of $|-\rangle$ polarized light for $\tau_d = 0$ (a), $\tau_d = $ -40 fs (b), $\tau_d = 40$ fs (c) and $\tau_d = 4$ ps (d).

To accurately determine the speed of wavefronts using this method, let $z_1 = 0.055$ m, $z_2 = 0.08$ m, and $\delta_2 = 1050\delta_1$ which is roughly the inhomogeneous broadening of the Nd^{3+} ions. Thus, the lower AOM in Fig. 2 may not be necessary. The propagation time in the first crystal is $t_1 \simeq z_1/v_0 \simeq 400$ ps. A time delay τ_d between the H polarized light and V polarized light is artificially introduced. Let $E_H(z_2,\omega) = \sqrt{1/2}E(0,\omega)Exp[ik_1(\omega)z_1]Exp[i\omega\tau_d]$. This means the H polarized light will fall behind (move ahead of) the V polarized light by $|\tau_d|$ for $\tau_d > 0$ ($\tau_d < 0$). The output intensities calculated using FFT with 0.1-ps sampling resolution with $\tau_d = 0$, -40 fs, 40 fs and 4 ps are shown in Figs. 4(a)-(d), respectively. Clearly I_- with $|\tau_d| = 40$ fs is much greater than that without delay. The longer the delay, the greater the I_- that can be obtained. Whether the H polarized light is faster or slower than the V polarized light has little effect on the output. This is shown in Fig.s 4(b) and 4(c). The sign of τ_d may be experimentally identified by introducing a compensation delay in either path.

Considering a realistic detector with a bandwidth of 5 GHz, the recorded power for $|-\rangle$ polarized light can be estimated by averaging the results in Fig. 4(b) for every 0.2 ns. The maximum outputs are $9.2 \times 10^{-11}, 2.5 \times 10^{-9}, 5.9 \times 10^{-10}$ and 6.6×10^{-6} for Figs. 4(a)-(d), respectively. The power of probe light can be chosen to be 1 mW in the experiment. Therefore, when the power of $|-\rangle$ polarized light is recorded with a value over 2.5 pW, we can conclude that there is a speed difference of $\Delta v > v_0/10^4$ for the two paths, which is approximately $\Delta v/v_0 \simeq \tau_d/t_1$. With the parameters chosen here, a bound of less than 10^{-4} on the accuracy of the wavefronts' speed can be experimentally determined.

The highest speed resolution with this scheme is not limited to 10^{-4} which depends on several parameters. The first is the rise time of the input pulse, which is determined by the modulation method. Because $I_- \propto \tau_d/t_r$, the smaller t_r is, the more sensitive I_- is to τ_d. The faster the signal rises, the harder they can "see" Nd^{3+} in the Nd^{3+}:YVO_4 crystal. The second is the length of the first crystal, z_1, which determines the transmission time, t_1. Because $\Delta v/v_0 \simeq \tau_d/t_1$, for a larger t_1, the speed difference can be determined more precisely. Third, detectors with better low-intensity responses can resolve a smaller τ_d. Note that the rise time of the detectors is not so important in this scheme because only the maximal intensity is of interest rather than the absolute time that the signal rises. Therefore, this method can determine the speed of the precursor to an accuracy of a given lower bound with better experimental conditions. Compared with previous works which determine the speed of information to an accuracy of about 0.1 by direct intensity recording [2, 27], our scheme shall give more accurate measurements.

To summarize, we propose an interference scheme for accurately measuring the speed of wavefronts in an optically pumped Nd^{3+}:YVO_4 crystal. The simulation results computed with linear susceptibility of EIT medium show that the arrival time of wavefronts is independent of the strong dispersions caused by Nd^{3+} ions. Considering the current available modulation and detection technologies, the pure YVO_4 crystal is treated as an infinite fast-response medium like the vacuum, so the wavefronts' speed we are measuring is v_0. In principle, with a powerful wideband filter and single-photon detectors with extremely low noise, the precursors which travel at the speed of c in a Nd:YVO_4 crystal also can be identified with our scheme. This scheme can be carried out in other systems where no background wideband medium is present, such as cold atoms and room temperature atoms. The conclusion can be made general as the ideal step-rising wave fronts travel at exactly the same speed c in all materials. This scheme provides an approach to accurately measure the arrival time of precursors in various systems with realistic detecting systems. Future experimental measurements will provide a strict test of whether the information velocity with medium violates the Einstein causality. This work bridges the gap between the ideal concepts of precursors and the real pulses with finite rise (fall) time by showing an accurate boundary.

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